

Stroke plane deviation for a microrobotic fly

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Abstract—Wing motion in most flapping-wing micro air vehicles (MAVs) is restricted to a flat stroke plane in order to simplify analysis and mechanism design. An MAV actuation and transmission design capable of controlling flapping motions and deviations from the mean stroke plane using relatively simple modifications to a proven design is presented. This allows preliminary investigation into more power-efficient wing trajectories, an important concern for small MAVs. A theoretical quasi-steady model of flapping wing flight is used to predict wing motions, and these predicted trajectories are compared to empirically observed trajectories from a test device.

I. INTRODUCTION

Within the last decade there has been increased interest in the area of flapping-wing micro air vehicles (MAVs) due to potential advantages over fixed-wing vehicles at small scales. Such vehicles range from larger bat and bird-sized ornithopters [1], [2], [3], [4] to smaller insect-sized vehicles and associated components [5], [6], including the Harvard Microrobotic Fly (HMF) [7], [8], [9], and even hybrid mechanical-biological systems [10]. The study of flapping-wing aerodynamics is a relatively new area, as the vast majority of flight vehicle research over the past 100 years has been in fixed or rotary wing aircraft. As such, engineers frequently look to flapping wing animals for design inspiration, especially with regards to morphology and motion. One frequent simplifying assumption is that the stroke plane is flat, i.e. the torsional axis of the wing flaps back and forth in a plane, and does not deviate vertically (Fig. 1 illustrates the wing motion and defines wing angles). There are two reasons for this assumption: (1) many biological wing trajectories do show relatively flat stroke planes, and (2) a flat stroke plane greatly simplifies mechanical construction, as a planar crank-rocker four-bar mechanism with a DC motor (or slider-crank with a linear piezoelectric actuator in the case of the HMF [11]) can be used to generate oscillatory wing motion; whereas stroke-plane deviation requires a more complicated three-dimensional mechanism or a spherical joint (such as the five-bar mechanism with auxiliary four-bar in [12]).

While the flat-stroke plane assumption seems to be a reasonable approximation and has proven successful for several MAV prototypes, inspection of biological data does reveal oval, U-shaped and figure-of-eight wing trajectories [13], [14], [15] (Fig. 2). Recent theoretical fluid dynamics studies of flapping-wing flight have shown that wing trajectories with nonzero stroke plane deviation may be more efficient and effective in terms of the power that must be expended

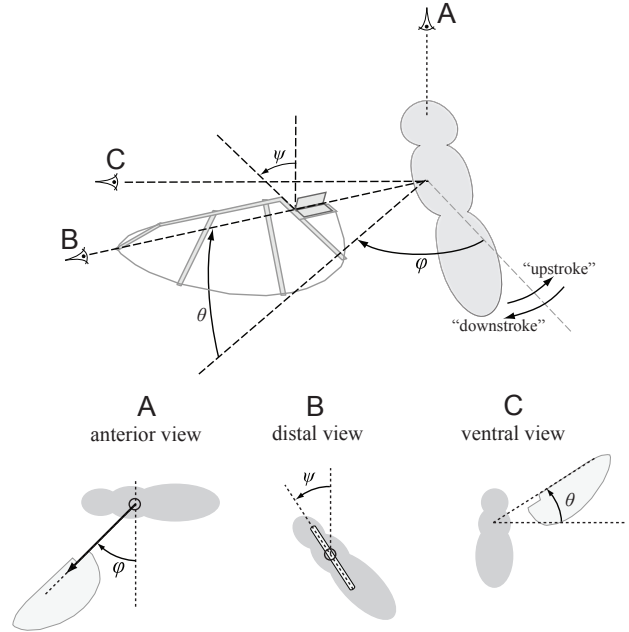


Fig. 1. Definitions of flapping-wing stroke parameters. The angle of rotation of the torsional axis of the wing measured about an axis perpendicular to the mean stroke plane is the *stroke angle* ϕ ; the out-of-plane angle measured to the torsional axis of the wing is the *deviation angle* θ ; and the rotation of the wing about its torsional axis is the *rotation angle* ψ . The wing flapping forward with respect to the body is referred to as the “downstroke”, flapping backward with respect to the body is the “upstroke”. Figure not to scale.

to keep the vehicle aloft or maneuver [16], [17]. Many current MAV designs have limited flight times due to the limited capacity and energy density of available small-scale power supplies [18], and the future of MAV flight depends heavily on improvement of energy sources such as Lithium-polymer batteries. Thus, any potential increase in efficiency is of vital importance. Since all previous HMF designs were restricted to flapping in a flat stroke plane, the investigation of potentially more efficient stroke trajectories involving stroke plane deviation was not possible. The new design presented here allows a preliminary comparison of different trajectory types based on the merits of lift generation and aerodynamic power expenditure as calculated by a theoretical blade-element aerodynamic model.

II. BACKGROUND AND PREVIOUS WORK

Unlike conventional aircraft which use separate control surfaces for decoupled roll, pitch and yaw control (i.e. elevators, ailerons and rudders), insects primarily use asymmetric

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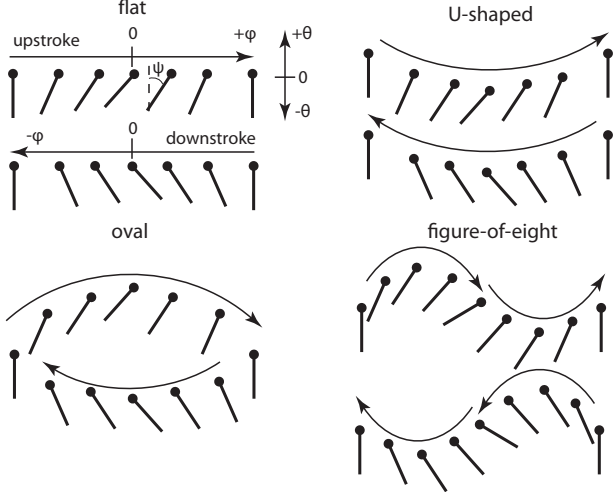


Fig. 2. An “unwrapped” distal view of nominal stroke types. Most MAVs have flat stroke planes, but many more varied trajectories are observed in nature. The filled-in circle represents the leading edge of the wing (assumed to be coincident with the torsional axis for this figure, although this need not be the case). Wing motion is parameterized by the angles ϕ , θ and ψ . For illustration purposes only, not to scale.

changes in wing kinematics for attitude control [19] (it has also been shown that insects can use abdominal and leg movements to aid in maneuvering [20], but that is beyond the scope of this work). Insects possess distinct groups of power and control muscles used to generate primary flapping motion and control these asymmetric motions respectively [21], [22], [23], [24]. Previous versions of the HMF have experimented with this idea, using a single large piezo-electric actuator to flap the wings, and smaller actuators to change the kinematics of the four-bar transmission, allowing asymmetric modulation of stroke amplitude [25], [26]. Since stroke-plane deviation angles are typically about an order of magnitude smaller than stroke amplitude (i.e. about 10 degrees compared to 100 degrees peak-to-peak), this also seems like a suitable application for separation of power and control actuators. Using previously developed fabrication techniques [27], a two-input transmission system consisting of two orthogonal flexure-based four-bars for actuation of stroke angle and deviation angle is constructed. Mechanism design, kinematic and dynamic analysis, and experimental results are presented in the following sections.

III. MECHANISM DESIGN AND FABRICATION

The original HMF transmission is a symmetric four-bar that converted a single linear actuator input into rotational motion of two wings. The flexure-based transmission, made from a layered combination of rigid carbon fiber sheets and flexible polymers, is laser-micromachined in two dimensions and then assembled into a three dimensional structure (Fig. 3). Flexures can either be fixed at 90 degrees using an adhesive, or left free to function as revolute joints. Previous modifications of this design to allow stroke amplitude modulation required additional actuator inputs but no topological

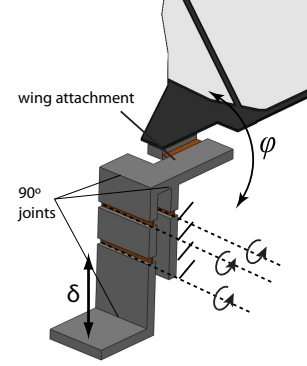


Fig. 3. Illustration of one-half of the original HMF transmission.

changes to the transmission [25], [26], however this design does not allow for stroke-plane deviation. It is desired to add a controlled degree of freedom with a rotation axis orthogonal to the ϕ rotation axis, while keeping the structure as simple as possible. This can be accomplished by adding a second flexure-based four-bar *orthogonal* to the original four-bar (Fig. 4). The two primary benefits of this design are that (a) it does not require any additional 90-degree folds, thus keeping fabrication simple and (b) if the flexures are stiff enough to off-axis loads (off-axis compliance must be considered when designing flexure-based mechanisms [28]), it gives decoupled control of stroke amplitude and deviation angle through two actuator inputs. Rotation of the wing remains passive as in the original HMF design, as opposed to previous MAV designs with direct control over both flapping and rotation [29], [30]. While there is still some debate as to the level of active or passive control of insect wing rotation, evidence exists to show that rotation is at least partially, if not wholly passive [31].

IV. KINEMATICS AND DYNAMICS

A. Kinematics

The kinematics of the four-bar mechanisms can be derived using a pseudo-rigid body model, assuming that all carbon fiber links are rigid and that flexures act as ideal revolute joints. This has been shown previously in [25], and the kinematics are reproduced here. The stroke angle ϕ can be written as a function of actuator input δ_1 and link geometry L_i (see Fig. 5):

$$L_y = L_1 + L_2 - L_4 \quad (1)$$

$$C_1 = L_3^2 + (L_2 - L_4)^2 - L_1^2 + L_3^2 \quad (2)$$

$$C_2 = 2\sqrt{L_3^2 + (L_2 - L_4)^2} \quad (3)$$

$$\phi = \cos^{-1} \left(\frac{(L_y - \delta_1)^2 + C_1}{C_2 \sqrt{L_3^2 + (L_y - \delta_1)^2}} \right) + \tan^{-1} \left(\frac{L_3}{L_y - \delta_1} \right) + \tan^{-1} \left(\frac{L_2 - L_4}{L_3} \right) - \frac{\pi}{2}. \quad (4)$$

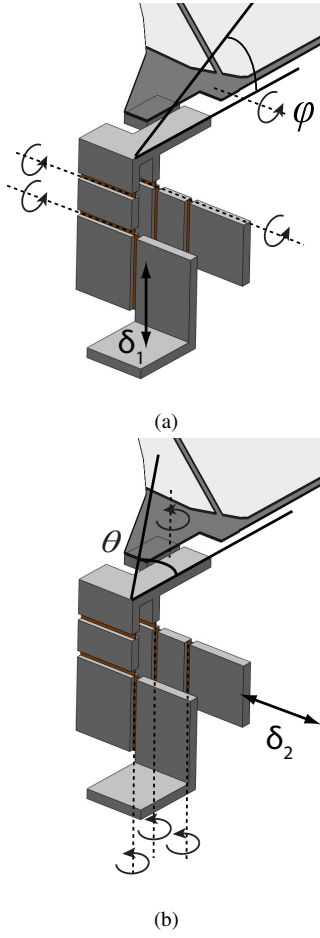


Fig. 4. Illustration of the stroke plane deviation transmission. Linear actuator inputs δ_1 and δ_2 are converted to (a) stroke angle ϕ and (b) deviation angle θ respectively. Note that this design does not require any additional 90 degree folds than the transmission in Fig. 3.

An equivalent formulation can be used to give θ as a function of actuator input δ_2 and the geometry of the second four-bar. Although Eq. 4 is nonlinear, geometry can be selected to give an approximately linear response [8] such that:

$$\phi \equiv T\delta_1 \quad (5)$$

where $T \approx 1/L_3$. Assuming an approximately linear relationship between input displacement and output angle allows the drive signals in Table I to be used to generate the baseline trajectories shown in Fig. 2, where A and B are the desired amplitudes for stroke angle and deviation angle respectively. Actual trajectories in ϕ – θ space are shown in Fig. 6 for given sinusoidal actuator inputs using the full nonlinear kinematics. It is important to note that these trajectories are not perfectly symmetric in ϕ or θ since the transmission kinematics are nonlinear and not symmetric about $\delta_i = 0$.

B. Dynamics

A linearized, lumped parameter dynamic model of the system is shown in Fig. 7. Each of the two actuator/transmission systems acts as a force source in parallel with a spring and

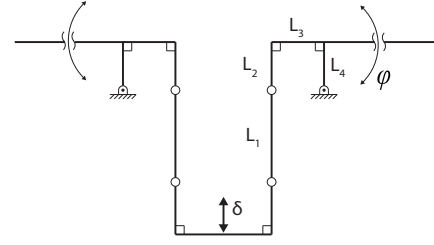


Fig. 5. A pseudo-rigid body model of the original transmission.

TABLE I
ACTUATOR DRIVE SIGNALS FOR DIFFERENT STROKE TRAJECTORIES

Trajectory	$\delta_1(t)$	$\delta_2(t)$
Flat	$\frac{A}{T} \sin(\omega t)$	0
Oval	$\frac{A}{T} \sin(\omega t)$	$\frac{B}{T} \sin(\omega t + \frac{\pi}{2})$
figure-of-eight	$\frac{A}{T} \sin(\omega t)$	$\frac{B}{T} \sin(2\omega t)$

damper element, which provide a linear input to a transmission that converts motion to wing rotation. Aerodynamic lift and drag forces (discussed below) act on the wing as a result of motion. It is important to note that, due to the orientation of the flexure hinge that allows the wing to passively rotate, the wing will not passively rotate when only δ_2 is actuated. Actuation of δ_1 is required to generate both lift and drag forces. The model used in this work is only a subsystem of the full dynamic model (inside the dashed box in Fig. 7), equivalent to assuming full kinematic control of δ_1 and δ_2 as control inputs. This allows focus on desired wing trajectories and resulting passive wing rotation. However, while the motions ϕ and θ are *kinematically* decoupled, it will be seen that they are not *dynamically* decoupled since actuation of δ_1 causes a force in the direction of δ_2 . While beyond the scope of this work, future dynamic modeling

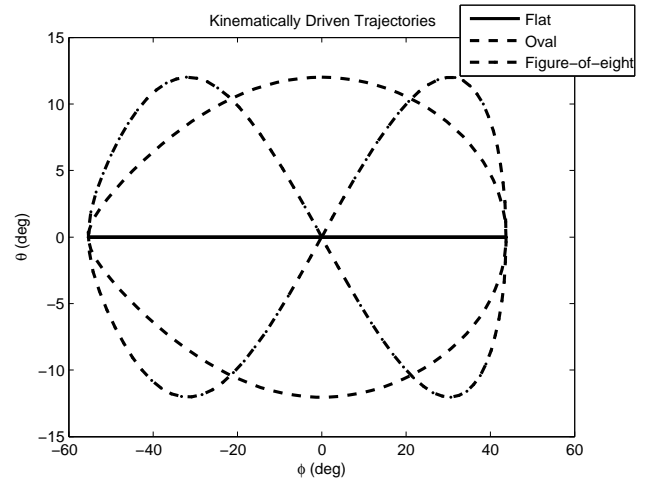


Fig. 6. Wing trajectories using the full nonlinear kinematics, with actuator inputs $\delta_1 = \pm 350\mu\text{m}$, $\delta_2 = \pm 100\mu\text{m}$, and transmission geometry $L_1 = 500\mu\text{m}$, $L_2 = 500\mu\text{m}$, $L_3 = 480\mu\text{m}$, $L_4 = 500\mu\text{m}$ for both the flapping and deviation transmissions.

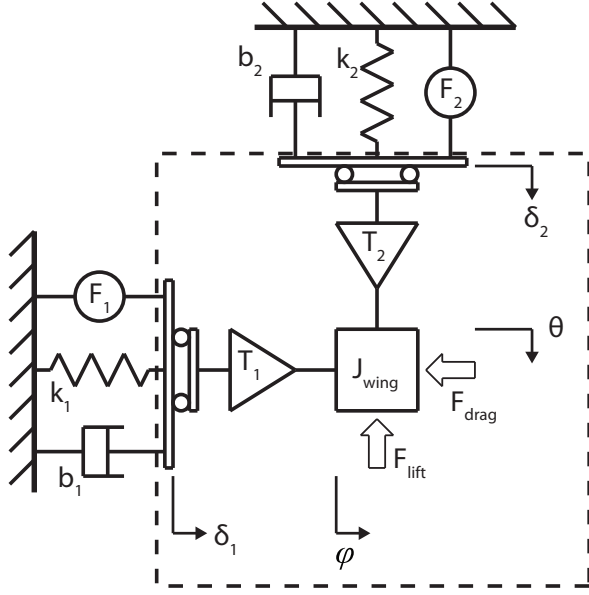


Fig. 7. A schematic of the system dynamic model. Only the subsystem within the dashed box is considered for purposes of this paper. Note that the motions δ_1 and δ_2 are (and therefore ϕ and θ) are kinematically decoupled.

will incorporate the spring-damper elements, with actuators modeled as force, not displacement sources.

The aerodynamic model is a quasi-steady blade element model, meaning that (a) lift and drag forces corresponding to the instantaneous wing velocity (derived empirically in [32]) are used and (b) aerodynamic forces and moments are calculated on thin chordwise strips of the wing, then integrated over the length of the wing to arrive at total forces and moments. Aerodynamic forces and moments are therefore functions of instantaneous wing velocity, angle of attack α (defined as the angle between the local translational velocity vector and the wing chord), and wing geometry. The wing is assumed to be a rigid flat plate attached to a torsional spring on the ψ -axis, rotations about the ϕ and θ axes are driven kinematically. A differential equation for ψ can then be written as a function of inertial, spring and aerodynamic terms and the driving (ϕ, θ) trajectory, of the form

$$\ddot{\psi} = f(\phi, \dot{\phi}, \theta, \dot{\theta}, \psi, \dot{\psi}, \mathbf{I}, M) \quad (6)$$

where \mathbf{I} is the wing's inertia tensor and M is the term including aerodynamic moments, which are functions of both normal and tangential force coefficients, wing geometry, and proportional to the square of wing velocity and rotation rate. The normal and tangential force coefficients C_N and C_T themselves are functions of α , thus the moment terms are of the form

$$M = f(C_N(\alpha), C_T(\alpha), \dot{\phi}^2, \dot{\theta}^2, \dot{\psi}^2, y(r), c(r)) \quad (7)$$

where $y(r)$ and $c(r)$ define the position of the leading edge and chord length of the wing as a function of radial position,

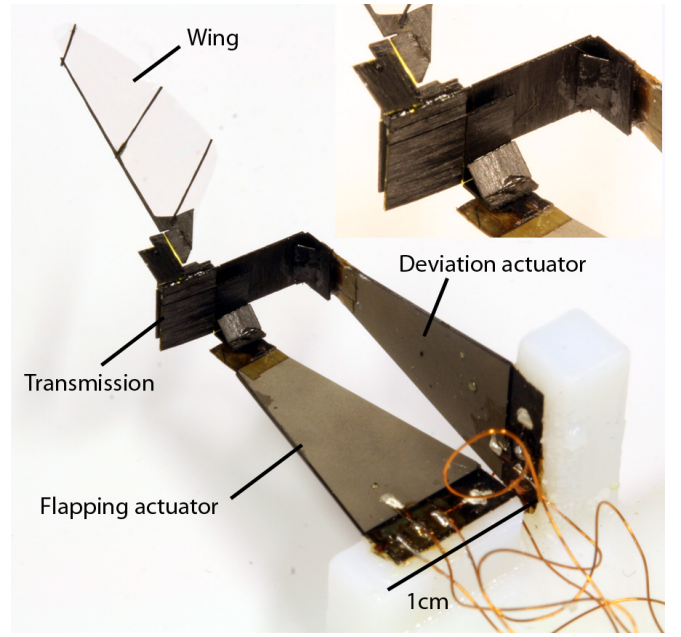


Fig. 8. The test structure used to collect data. Actuator control signals are supplied externally. (inset) A closer view of the transmission.

thus fully defining the planar wing shape. The the reader is referred to [33] for detailed derivation and explanation of the exact form and individual terms in Eqs. 6 and 7.

V. EXPERIMENT

A. Methods

A test device using the transmission shown in Fig. 4 with two externally powered piezoelectric actuators and a wing connected to the output link was constructed (Fig. 8). Note that on-board power supply and electronics for the HMF are ongoing research areas [34], [35], but not considered for the tests presented here. Piezoelectric actuators were driven with a custom Matlab program (Mathworks Inc.). 0-5V range analog signals output from the computer were amplified to levels required to drive the actuators (200-300V) with a high-voltage amplifier (Trek Inc.). Wing motion was filmed using two Phantom V7.3 high-speed cameras (Vision Research) oriented at approximately 90° to each other. Two-dimensional coordinates of points on the wing were extracted from the left and right camera views separately using 2D motion tracking software (ProAnalyst from Xcitex Inc.). The use of two cameras allowed stereoscopic reconstruction of full three-dimensional wing kinematics [36]. Note that the calibration procedure calculates the relative camera positions and orientations, so the camera positions need not be exactly known *a priori*. Still images from two sample videos are shown in Fig. 9.

B. Results

Three trajectory types are tested: flat, oval, and figure-of-eight. Trajectories are driven with the actuator signals presented in Table I. All three wing angles are plotted as

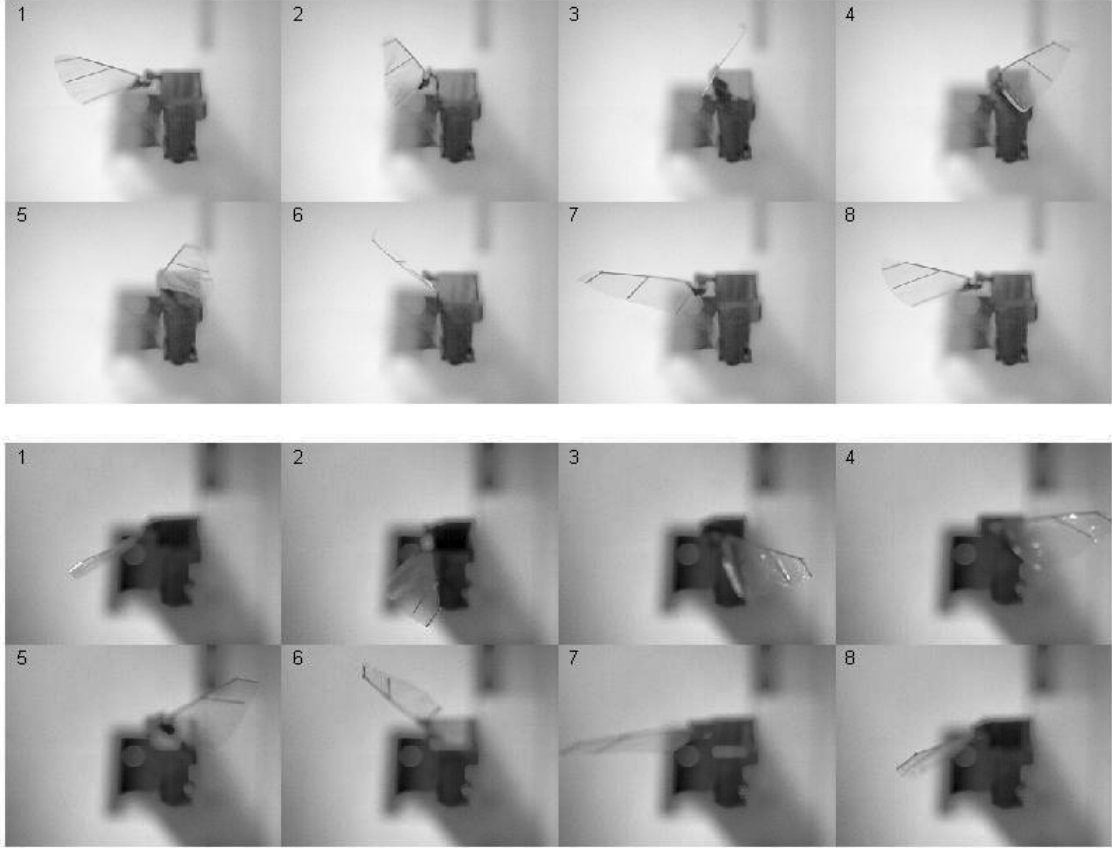


Fig. 9. Still images from one camera for flat (top) and oval (bottom) stroke trajectories. Data was recorded at 5000fps, so 50 data points were collected per cycle flapping at 100Hz. Every 7th frame for one cycle is shown, the time between images is 1.4msec.

functions of time in Figure 10, however visualizing the shape of each trajectory is easier when viewing a plot of θ vs. ϕ (Fig. 11). One can imagine this as approximately the wingtip trajectory that would be seen with an edge-on view of the wing mapped from the surface of a sphere.

It is immediately evident that the experimental data, while qualitatively similar in shape, does not match the example trajectories displayed in Fig. 2. However, when driven at low frequencies - i.e. when aerodynamic and inertial forces are negligible - a reasonable figure-of-eight trajectory, similar to the kinematically predicted trajectory in Fig. 6, can be obtained (Figs. 10d and 11d). There are two possible sources of error. First, the compliance of the stroke-plane-deviation actuator and transmission (k_2 in Fig. 7) allows unexpected vertical motions of the wing due to coupling of the lift force, as there is no feedback system in place to reject disturbances in this direction. Second, the transmission design relies heavily on the idea that flexure joints will act as ideal revolute joints, with one axis of rotation and infinite off-axis stiffness. In practice this is not true [28], and off-axis compliance of the flexure joints can lead to undesired motion.

Despite the fact that the observed trajectories are not as consistent as hoped, experimental results can still be compared to the aerodynamic model in [33] in order to make a preliminary comparison of efficiency. Fig. 12 shows

TABLE II
THEORETICAL AERODYNAMIC LIFT, POWER AND EFFICIENCY FOR
THREE OBSERVED WING TRAJECTORIES

Trajectory	Avg. Lift (mN)	Avg. Power (mW)	Lift/Power (N/W)
Flat	.67	3.29	.20
Oval	1.59	14.0	.11
Fig. 8	1.54	10.4	.15

experimental and predicted passive rotation for the recorded flapping and deviation kinematics. Average lift, average aerodynamic power, and lift/power (all theoretical values calculated with the model in [33], as lift and aerodynamic power are not measured directly) as a measure of efficiency are compared for each trajectory (Table II). It is seen that the flat trajectory actually has the best lift/power ratio, and that the figure-of-eight trajectory requires less power to generate about the same amount of lift as the oval trajectory. Note that the flat trajectory actually has a slight figure-of-eight shape to it; thus introducing the possibility that a passive figure-of-eight could be more efficient than an actuated figure-of-eight. However, the data presented here is not extensive enough to draw any definitive conclusions on the most efficient type of wingstroke.

VI. CONCLUSIONS

The work presented here is intended as a preliminary exploration into actuated stroke-plane deviation for a micro-

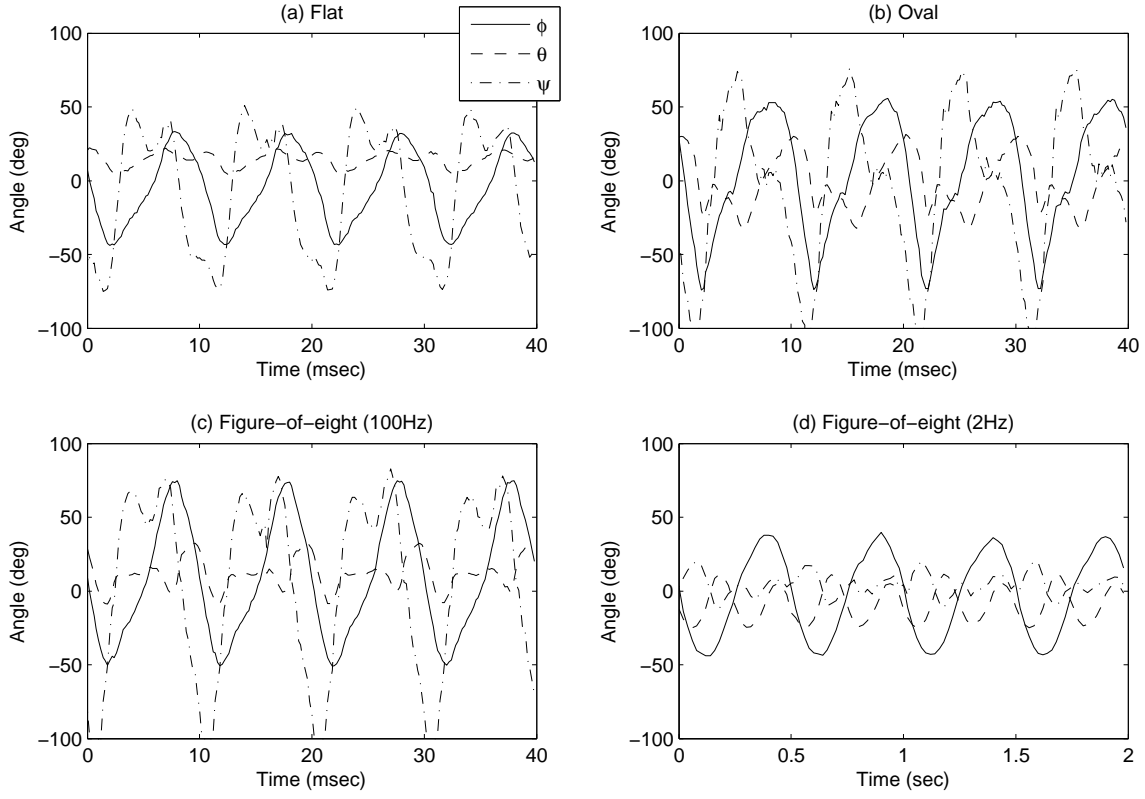


Fig. 10. Experimental wing angles vs. time for (a) a nominally flat trajectory, (b) an oval trajectory, (c) a figure-of-eight, all at 100Hz and (d) a figure-of-eight at 2Hz.

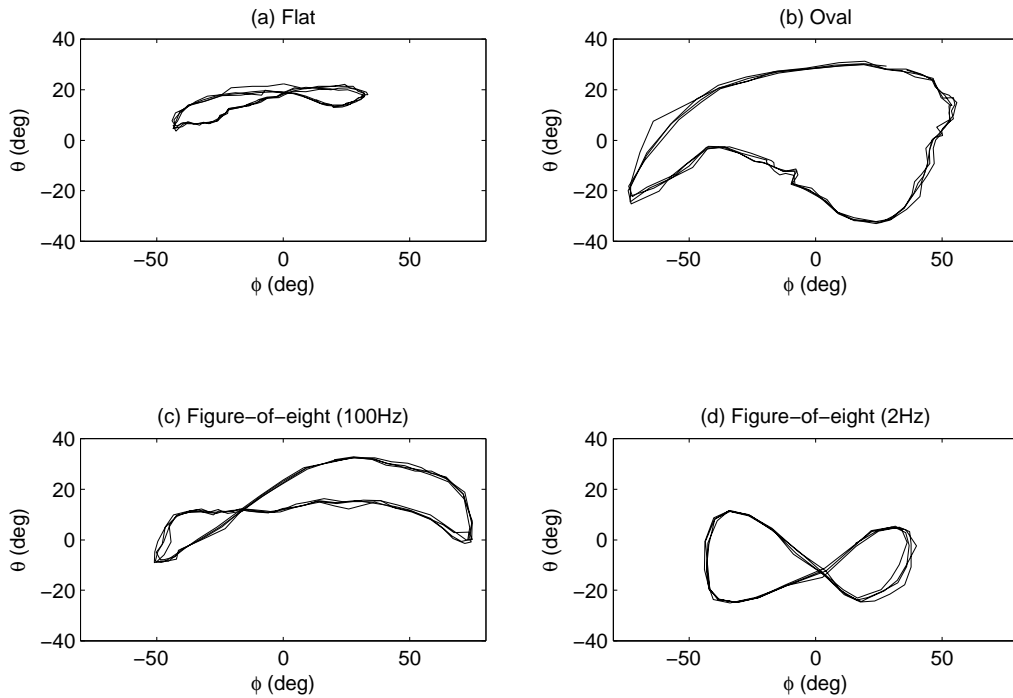


Fig. 11. θ vs ϕ for each of the four experimental trajectories, corresponding to Fig. 10.

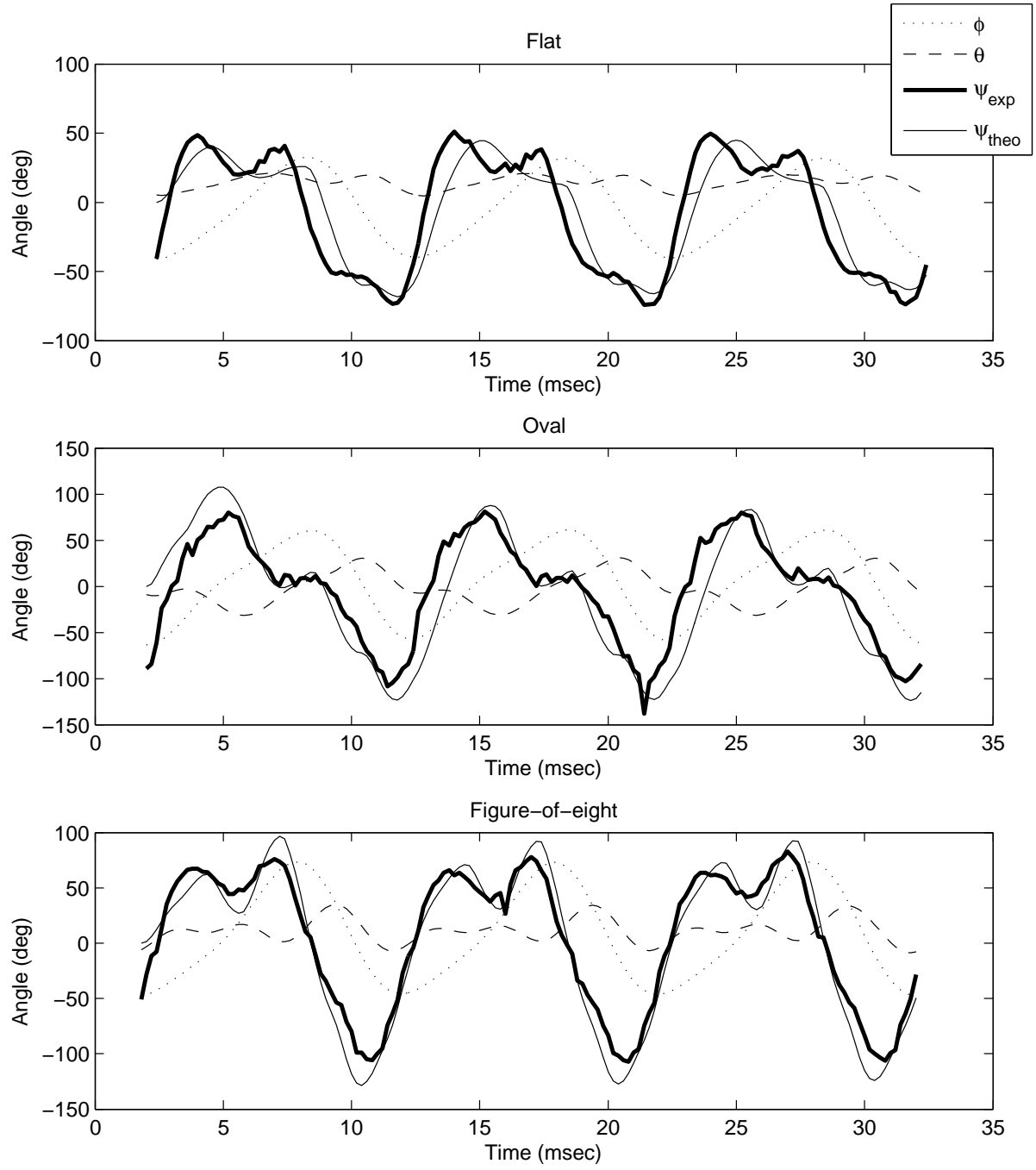


Fig. 12. Experimental flapping and deviation angles ϕ and θ plotted with experimental and theoretical rotation angles ψ_{exp} and ψ_{theo} .

robotic fly, due to potential gains in efficiency; not a full attempt to tackle the multidimensional optimization problem of an optimal wing trajectory and associated mechanical drive system. Potential use of stroke plane deviation as a control method for vehicle maneuvering and stability has not been investigated, but will be the subject of future work. The authors do *not* make the claim that a given trajectory type is more efficient than another based on the preliminary results presented here. Much further work, both theoretical and experimental, will be required to make any claim of an optimal trajectory. Most aerodynamic studies, such as [17] and [33] assume kinematic control of wing motion, without considering actuator or transmission dynamics. The results here show that actuator/transmission dynamics and compliance play a vital role in resultant trajectories, and re-evaluation of the transmission structure along with further dynamic modeling is required. Additional experimental measurements may also be made to evaluate the lift/power criteria. Lift force can be measured directly as in [33], [37] and compared to theoretical values. While it is difficult to experimentally measure aerodynamic power, electrical power input to the actuators can be measured directly and used as a criteria. Additional work in all of these areas will allow development of wing trajectories and thorax designs for increased maneuverability and flight times of insect-sized MAVs.

VII. ACKNOWLEDGEMENTS

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